

**Problem 1.** Solve the equation  $3^x + 9^x = 27^x$ .

**Problem 2.** An equilateral triangle is inscribed in a circle of area  $1m^2$ . Then the second circle is inscribed in the triangle. Find the radius of the second circle.

**Problem 3.** Solve the inequality:

$$2\sqrt{x^2 - 5x + 4} + 3\sqrt{x^2 + 2x - 3} \geq 5\sqrt{6 - x - x^2}.$$

**Problem 4.** Peter and John played a game. Peter wrote on a blackboard all integers from 1 to 18 and offered John to choose 8 different integers from this list. To win the game John had to choose 8 integers such that among them the difference between any two is either less than 7 or greater than 11. Can John win the game? Justify your answer.

**Problem 5.** Prove that given 100 different positive integers such that none of them is a multiple of 100, it is always possible to choose several of them such that the last two digits of their sum are zeros.

**Problem 6.** Given 100 different squares such that the sum of their areas equals  $1/2 m^2$ , is it possible to place them on a square board with area  $1 m^2$  without overlays? Justify your answer.